

【中2数学 | 連立方程式】

1、次の連立方程式を解きなさい。

$$\square(1) \begin{cases} \frac{2}{3}x - \frac{1}{2}y = -5 & \dots \textcircled{1} \\ -\frac{x}{2} + y = 5 & \dots \textcircled{2} \end{cases}$$

$\textcircled{1} \times 6$ より、 $4x - 3y = -30 \dots \textcircled{1}'$
 $\textcircled{2} \times 2$ より、 $-x + 2y = 10 \dots \textcircled{2}'$
 $\textcircled{1}' + \textcircled{2}' \times 4$ より、
 $5y = 10 \therefore y = 2$
 $\textcircled{2}'$ に代入
 $-x + 4 = 10 \therefore x = -6, y = 2$
 $\therefore x = -6$

$$\square(3) \begin{cases} \frac{2x-3y}{4} = 3 & \dots \textcircled{1} \\ \frac{2}{3}x + \frac{y}{2} = 1 & \dots \textcircled{2} \end{cases}$$

$\textcircled{1} \times 4$ より、 $2x - 3y = 12 \dots \textcircled{1}'$
 $\textcircled{2} \times 6$ より、 $4x + 3y = 6 \dots \textcircled{2}'$
 $\textcircled{1}' + \textcircled{2}'$ より、
 $6x = 18 \therefore x = 3$
 $\textcircled{2}'$ に代入
 $12 + 3y = 6 \therefore y = -2$
 $\therefore x = 3, y = -2$

$$\square(5) \begin{cases} \frac{x}{4} - \frac{y}{3} = 5 & \dots \textcircled{1} \\ \frac{2}{3}x + \frac{x-2y}{2} = 20 & \dots \textcircled{2} \end{cases}$$

$\textcircled{1} \times 12$ より、 $3x - 4y = 60 \dots \textcircled{1}'$
 $\textcircled{2} \times 6$ より、 $4x + 3x - 6y = 120$
 $7x - 6y = 120 \dots \textcircled{2}'$
 $\textcircled{1}' \times 3 - \textcircled{2}' \times 2$ より、
 $-5x = -60 \therefore x = 12$
 $\textcircled{1}'$ に代入
 $36 - 4y = 60 \therefore y = -6$
 $\therefore x = 12, y = -6$

$$\square(2) \begin{cases} \frac{x}{2} + \frac{y}{3} = 7 & \dots \textcircled{1} \\ \frac{3}{4}x - \frac{2}{5}y = -3 & \dots \textcircled{2} \end{cases}$$

$\textcircled{1} \times 6$ より、 $3x + 2y = 42 \dots \textcircled{1}'$
 $\textcircled{2} \times 20$ より、 $15x - 8y = -60 \dots \textcircled{2}'$
 $\textcircled{1}' \times 4 + \textcircled{2}'$ より、
 $27x = 108 \therefore x = 4$
 $\textcircled{1}'$ に代入
 $12 + 2y = 42 \therefore y = 15$
 $\therefore x = 4, y = 15$

$$\square(4) \begin{cases} \frac{1}{2}x - \frac{3}{4}y = 1 & \dots \textcircled{1} \\ \frac{5x+2}{3} = \frac{y}{2} & \dots \textcircled{2} \end{cases}$$

$\textcircled{1} \times 4$ より、 $2x - 3y = 4 \dots \textcircled{1}'$
 $\textcircled{2} \times 6$ より、 $10x + 4 = 3y$
 $10x - 3y = -4 \dots \textcircled{2}'$
 $\textcircled{1}' - \textcircled{2}'$ より、
 $-8x = 8 \therefore x = -1$
 $\textcircled{1}'$ に代入
 $-2 - 3y = 4 \therefore y = -2$
 $\therefore x = -1, y = -2$

$$\square(6) \begin{cases} \frac{3x-y}{6} - \frac{2}{3}x = 1 & \dots \textcircled{1} \\ \frac{1}{2}x - \frac{3}{4}y = 2 & \dots \textcircled{2} \end{cases}$$

$\textcircled{1} \times 6$ より、 $3x - y - 4x = 6$
 $-x - y = 6 \dots \textcircled{1}'$
 $\textcircled{2} \times 4$ より、
 $2x - 3y = 8 \dots \textcircled{2}'$
 $\textcircled{1}' \times 2 + \textcircled{2}'$ より、
 $-5y = 20 \therefore y = -4$
 $\textcircled{1}'$ に代入
 $-x + 4 = 6 \therefore x = -2$
 $\therefore x = -2, y = -4$